

BITS,Pilani-Dubai

2<sup>nd</sup> Semester,2010-11

Course Title/Course No.: ELECTROMAGNETIC FIELDS AND WAVES ( EEE C433 )

IIIrd Year( EEE) Comprehensive Examination

( F.M-80, Weightage—40%) Date— 29/05/2011 ; Duration—3 Hours.

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(1) In free space with  $\epsilon_0 = 8.854(10^{-12})$  F/m and  $\mu_0 = 4\pi(10^{-7})$  H/m, it is given that  $\vec{E} = C \sin(12y) \sin(az) \cos\{2(10^{10})t\} \vec{1}_x$  Volts/meter for a region where "C" and "a" are unknown. Using Maxwell's equations find numerical value for the coefficient "a" where  $a > 0$ . [12 marks]

(2) A 2.0 GHz uniform plane wave has an amplitude,  $E_{y0} = 1.4$  kv/meter and it is propagating in the  $\vec{1}_z$  direction. The given data are :  $\epsilon' = 3.0(10^{-11})$  F/m,  $\epsilon'' = 1.6(10^{-11})$  F/m,  $\mu = 2.5(10^{-6})$  F/m. Calculate: (a)  $E_y$  at (0, 0, 1.8 cm) at  $t = 0.2$  ns (b)  $H_x$  at (0, 0, 1.8 cm) at  $t = 0.2$  ns [5+3 marks]

(3)(a) In context to "Wave propagation in Dielectrics", use the standard expression for intrinsic impedance. Considering the case of a conductive material having conductivity, " $\sigma$ ", after necessary mathematical derivation, prove that " $\sigma$ " can be expressed as  $\sigma = \omega \epsilon''$ .

(b) Consider the case of Reflection and Refraction phenomena of uniform plane wave propagation. It is given that region-1 is a perfect dielectric and region-2 is a perfect conductor. The uniform plane wave in region-1 is normally incident on the planar boundary separating region-1 and region-2. After necessary mathematical derivation and using the findings of question 3(a), establish that "**NO TIME VARYING MAGNETIC FIELD CAN EXIST IN REGION-2**".  
-----[6+6 marks]

(4) With reference to "Transmission Lines of Finite Length", one receiver of 200 ohm resistance value is connected in parallel with a capacitive impedance of  $-j300$  ohm. This resistance-capacitance combination is treated as a load for the transmission line having a length of 4.0 meter. Characteristic Impedance ( $Z_0$ ) of the transmission line is 300 ohm. Source(operating) frequency is 100 MHz and velocity of propagation is  $2.5(10^8)$  m/sec. Calculate: (a) Reflection Coefficient ( $\Gamma$ ); (b) V.S.W.R (c) Input Impedance ( $Z_{in}$ ) (both magnitude and phase) (d) Source Current(in polar form) for a source voltage of 50 volts and Thevenin impedance of  $250 + j0$  ohm.---- [12 marks]

[P.T.O]

(5) Develop the "**SMITH CHART**" ( properly labeled diagram) of Transmission line after deriving all equations in detail. Initiate the analysis using the relation,  $\Gamma = (Z_L - Z_0) / (Z_L + Z_0)$ -- [9+4 marks]

(6) A uniform plane wave in region-1 is normally incident on the planar boundary separating region-1 and region-2. If  $\epsilon_1'' = \epsilon_2'' = 0$ , while  $\epsilon_{r1}' = (\mu_{r1})^3$  and  $\epsilon_{r2}' = (\mu_{r2})^3$ , find the ratio " $(\epsilon_{r2}' / \epsilon_{r1}')$ " if 20% energy in the incident wave is reflected at the boundary. There are two possible answers.----- [8 marks]

(7) In context to a "**Parallel Plate Wave-Guide**", prove that Group Velocity,  $v_{gm}$  can be expressed as  $v_{gm} = (c/n) \sin \theta_m$ , where the symbols have their usual meaning. [7 marks]

(8) Draw the labeled diagram of a "**Transmitting Antenna**" showing all the regions and also draw the labeled diagram of "**Antenna Field Pattern(Radiation)**" showing  $r, \theta, \phi$  coordinates.--  
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IIIrd Year( EEE) Test-2(OPEN BOOK) ( F.M-20, Weightage—20%) /Date—15/05/2011

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Marks distribution: Q1)—9 Marks, Q2)—6 Marks Q3)—5 Marks

**Instructions: Prescribed Text Book and handwritten notes only will be allowed**

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- (1) The incident voltage wave on a certain lossless transmission line for which  $Z_0 = 50.0$  ohms and phase velocity  $(v_p) = 2(10^8)$  m/s is  $V^+(z,t) = 200 \cos(\omega t - \pi z)$  volts. (a) Find  $\omega$  (b) Find  $I^+(z,t)$ . The section of line for which  $z > 0$  is replaced by a load  $Z_L = 50.0 + j 30.0 \Omega$  at  $z = 0$ . Find : (c) Reflection Coefficient ( $\Gamma$ ); (d)  $V_s(z)$ ; (e)  $V_s$  at  $z = -2.2$  metre
  - (2) In context to "Polarization", given a wave for which  $E_s = 15 e^{-j\beta z} \vec{1}_x + 18 e^{-j\beta z} e^{j\phi} \vec{1}_y$  Volts/meter in a medium characterized by complex intrinsic impedance,  $\eta$  : (a) Find the expression for  $H_s$ , involving the term " $\eta$ "; (b) determine the average power density in  $W/m^2$  (involving the term " $\eta$ " or associated term)
  - (3) A 1 MHz uniform plane wave [ in free space with  $\epsilon_0 = 8.854(10^{-12})$  and  $\mu_0 = 4\pi(10^{-7})$  ] is normally incident onto a freshwater lake ( $\epsilon_r' = 78$ ,  $\epsilon_r'' = 0$ ,  $\mu_r = 1$ ). Determine the fraction of incident power that is (a) reflected and (b) transmitted. (c) Determine the amplitude of electric field ( as a fraction of  $E_{x10^4}$ ) that is transmitted into the lake
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IIIrd Year( EEE) Test-1 ( F.M-25, Weightage—25% ) /Date—27/03/2011

Duration = 50 min.

Marks distribution: Q1)—9 Marks, Q2)—6+2+1 Marks Q3)—7 Marks

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- (1) A 50-cm. long wire is aligned with the positive x-axis direction. This wire moves in a plane represented by the equation :  $z=3$  meter, with a velocity expressed as  $\vec{v}=2\vec{i}_x+4\vec{i}_y$  meter/sec. in a magnetic field. This magnetic field has a vector potential expressed as  $\vec{A}=(6z+3xyz^2)\vec{i}_x+6\vec{i}_y+(3x^2yz)\vec{i}_z$  Webers/meter. Calculate the e.m.f induced in the wire.
- (2) Based on Maxwell's equations derive the Poynting's Theorem( with mathematical steps in detail) and hence establish the expression for the Poynting Vector. Also state the physical significance of each term in the right hand side of the above-said theorem.
- (3) Let  $jk = 0.2 + j1.5 \text{ m}^{-1}$  and  $\eta = 450 + j60 \Omega$  for a uniform plane wave propagating in the  $\vec{i}_z$  direction. If  $\omega = 300 \text{ Mrad/s}$ , find  $\mu$ ,  $\epsilon'$ , and  $\epsilon''$  for the medium.
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[SET- A]

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2<sup>nd</sup> Semester, 2010-11 -----Name of the student/Id No.-----

IIIrd Year( EEE) Quiz-II ( F.M-14, Weightage—7%) (Set- A) /Date—20/04/2011

Marks distribution: Q3)—2 Marks, and other questions of 3 Marks each

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1.) Given that  $Z_L = 150 \text{ ohm}$  and  $Z_0 = 300 \text{ ohm}$ . Calculate "Reflection Coefficient" and "V.S.W.R"

2.) Given that  $Z_L = 150 \text{ ohm}$  and  $Z_0 = 300 \text{ ohm}$  and  $\beta l = 1.6\pi$  radians. Calculate Input Impedance( $Z_{in}$ ).

3.) Prove that the Transmission Coefficient( $\tau$ ) can be expressed as  $\tau = 2Z_L / (Z_0 + Z_L)$

[P.T.O]

SET-A

Name/Id No. - - - - -

4.) In a transmission line, the following relation is given:

$\Delta V / \Delta Z = -[RI + L(\partial I / \partial t) + (1/2) L(\partial \Delta I / \partial t) + (1/2) (R\Delta I)]$ , where the symbols have their usual meanings.

Assuming that  $\Delta Z$  approaches zero, prove that :

$$\partial V / \partial Z = -[RI + L(\partial I / \partial t)] .$$

5.) Draw the labeled diagram of Smith Chart.

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Duration = 20 min.

IIIrd Year( EEE) Quiz-I ( F.M-16, Weightage—8% ) (Set- A) /Date—02/03/2011

Marks distribution: Q1)—1 Mark, Q7)—3 Marks and other questions-- 2 Marks each

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- 1.) Prove that the unit of POYNTING VECTOR will be Watts /m<sup>2</sup>. [1 Mark]
- 2.) Fill in the blank:  $\vec{\nabla} \cdot (\vec{E} \times \vec{H}) = \text{-----} + \vec{H} \cdot (\vec{\nabla} \times \vec{E})$  [2 Marks]
- 3.) It is given that,  $\vec{\nabla} \times \vec{H} = \epsilon_0 \left( \frac{\partial \vec{E}}{\partial t} \right)$ . What will be the value of conduction current density in such case? Show necessary mathematical formulations.
- 4.) Fill in the blank, showing the concerned derivations:  $(\mu \vec{H} \cdot \frac{\partial \vec{H}}{\partial t}) = \frac{\partial}{\partial t} (\text{-----})$
- 5.) Between the two plates of a capacitor, there is no electrical connection. Still current flows due to external voltage supply to the capacitor. How does it happen without electrical connection? Explain mathematically using electromagnetic field equations either in Differential form or in Integral form.
- 6.) Write the wave equation of a uniform plane wave (T.E.M) in free space and write the name of each symbol. Which is the direction of wave propagation in the equation written?

[P.T.O]

- 7.) A capacitor is energized from a voltage source,  $V = V_0 \cos \omega t$ . The following are given:  
S=Surface area of capacitor ;  $\epsilon$  = Permittivity of the dielectric medium ; d= Separation distance between the parallel plates of the capacitor;  $\omega$  =Supply frequency in electrical radians /second;

Derive the expression for Displacement Current using the concept of Displacement Current Density.

- 8.) Write the necessary field equations (only) to reach the formulation for the Vector Helmholtz equation in free space. No complete derivation is necessary.
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