

**BITS PILANI DUBAI CAMPUS**  
**Knowledge Village, Dubai**  
**I Semester 2005-06**

Course No: ES UC221

Date:

Max Marks: 20

Test 1- Regular (Make Up)

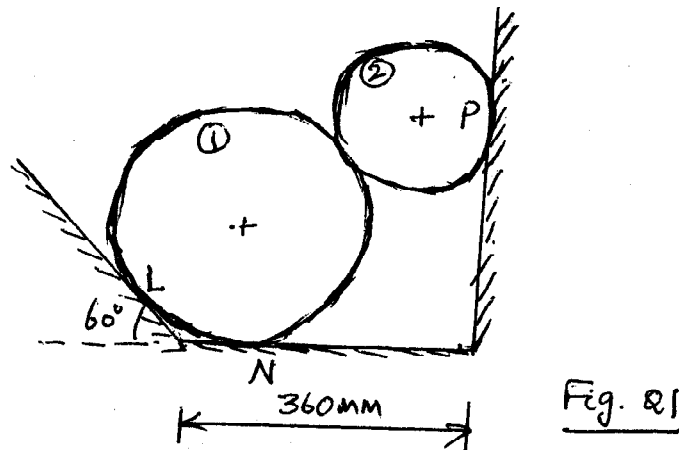
Course title: Mechanics of Solids

Duration: 50 Min

Weightage: 20%

Q1. Two cylinders 1 and 2 rest in a horizontal channel as shown in Fig. Q1. The cylinder 1 has a height of 500 N and a radius of 180 mm. The cylinder 2 has a height of 200 N and a radius of 100 mm. The channel is 360 mm wide at the bottom with one side vertical. The other side is inclined at an angle of  $60^\circ$  with the horizontal. Find the reactions (i) of the channel wall at the point P, (ii) of cylinder 1 on cylinder 2, (iii) of bottom surface at the point N, (iv) channel wall at L on the cylinder

[6 Marks]



Q2. A rigid beam AC is supported at its left end A by a pin. At its right end C it is supported by another rigid bar CF, which is in turn supported by an aluminum rod at D and a steel rod at E. Before any loads are applied the rigid bars both are level. A known load P is applied at point F and an unknown load Q at point B. Find Q in terms of P if the rigid bar CF is to be level after the two loads are applied. Refer Fig. Q2

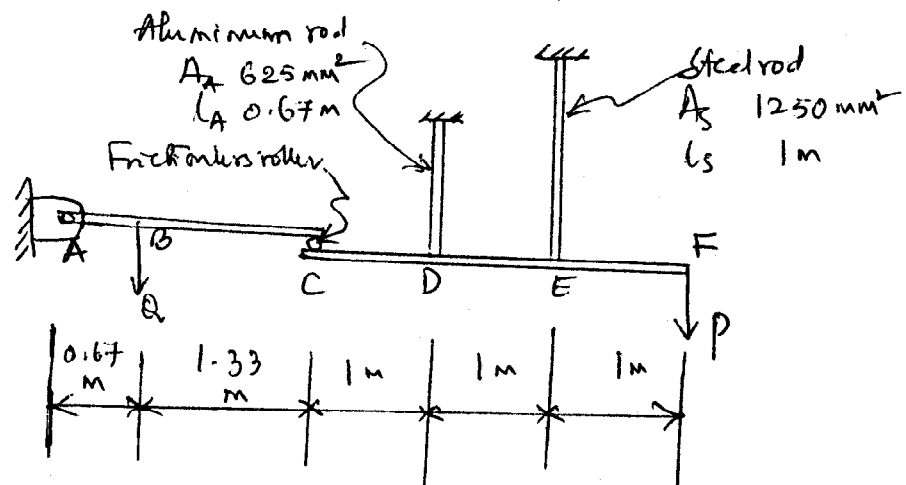


Fig. Q2

[6 Marks]

Q3. A tower used for a highline is shown in the Fig. Q3. If it is subjected to a horizontal force of 600 kN, then determine the forces in all the members

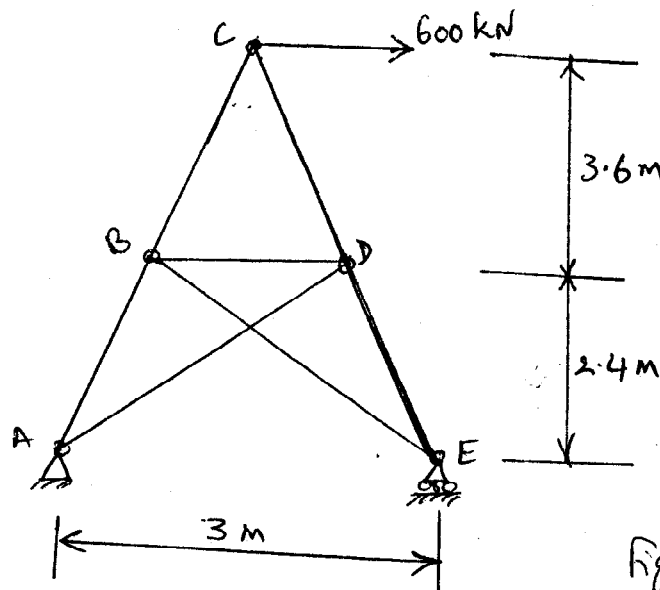


Fig Q3 [4 Marks]

Q4. A block A weighing 100 N rests on a rough inclined plane whose inclination to the horizontal is  $45^\circ$ . This block is connected to another block B weighing 300 N resting on a rough horizontal plane by a weighing rigid bar inclined at an angle of  $30^\circ$  to the horizontal. Find the horizontal force required to be applied to the block B to just move the block A in upward direction. Take the coefficient of static friction as 0.268 at all surfaces where there is sliding.

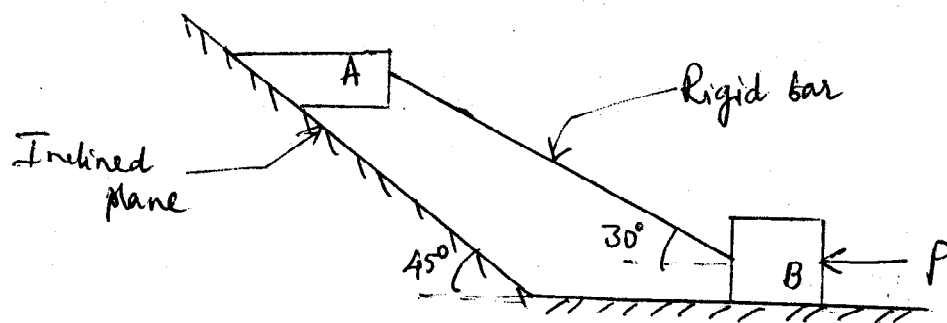


Fig Q4

[4 Marks]

**BITS PILANI DUBAI CAMPUS**  
**Knowledge Village, Dubai**  
**I Semester 2005-06**

Course No: ES UC221  
 Date:  
 Max Marks: 20

Test 2- Make up (Open Book)

Course title: Mechanics of Solids  
 Duration: 50 Min  
 Weightage: 20%

Q1. For the case shown in Fig. Q1, sketch the shear force and bending moment diagrams. Indicate sign convention employed and label important values. [8]

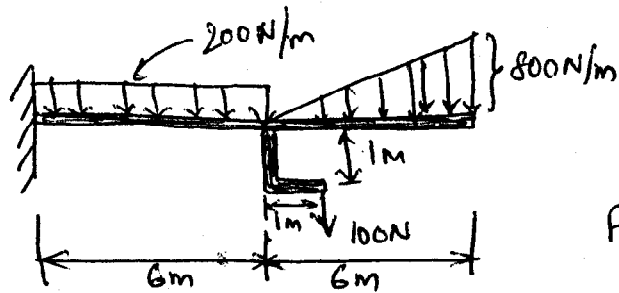


Fig. Q1

Q2. Given the following state of plane stress at a point

$$\sigma_x = -40 \text{ MPa} \quad \sigma_y = 20 \text{ MPa} \quad \tau_{xy} = 40 \text{ MPa}$$

- Justify whether is it possible to get a normal stress of -20 MPa and a positive shear stress at this point?
- If so, at what angle x-axis should be rotated to get the above state of stress given in (i).

[5]

Q3. Given the following state of plane stress at a point,

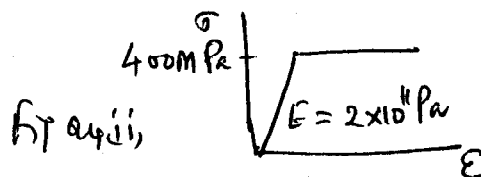
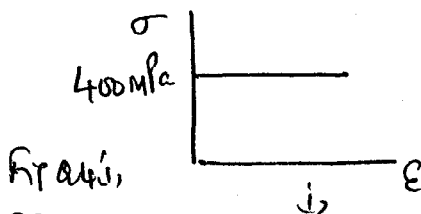
$$\sigma_x = 20 \text{ MPa} \quad \sigma_y = 40 \text{ MPa} \quad \tau_{xy} = -10 \text{ MPa}$$

- What are the principal strains in the xy plane?
- Find the strains at axes rotated  $30^\circ$  clockwise from xy axes.

Modulus of Elasticity=200 GPa and poisson's ratio=0.3

[5]

Q4. Shown in Fig. Q4 (i) perfectly plastic and Fig. Q4 (ii) is elastic perfectly plastic stress-strain idealizations. What stress is needed in each case to have a strain of 0.0005?



[1]

Q5. The principal stresses at a point are

$$\sigma_1 = 50 \text{ MPa} \quad \sigma_2 = 40 \text{ MPa} \quad \sigma_3 = 10 \text{ MPa}$$

What is the maximum shear stress at this point?

[1]

# BITS PILANI DUBAI CAMPUS

First Semester 2005-06

## COMPREHENSIVE EXAMINATION (CLOSED BOOK)

Course Name: Mechanics of Solids

Date: 04.01.2006

Max Marks: 40

Course No: ES UC221

Weightage: 40%

Duration: 3Hrs

Note: Answer Part A, Part B and Part C in separate answer books

### PART A

Q1. On a concrete ramp (Figure Q1) a force "F" is required to (i) start pushing a block up when the slope is  $30^\circ$  and (ii) hold it from sliding back when the slope is  $60^\circ$ . What is the coefficient of static friction between the block and concrete?

[4M]

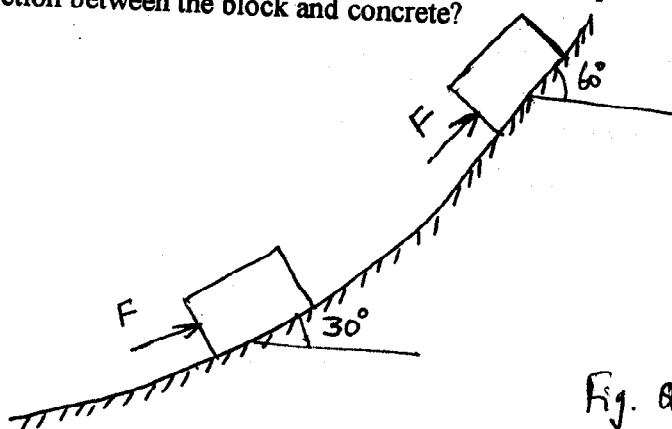


Fig. Q1

Q2. In the pin-jointed cantilever truss shown in Fig. Q2, all the members have a cross sectional area  $A=5000 \text{ mm}^2$ , and elastic modulus  $E=200 \text{ GN/m}^2$ . Find:  
(i) the forces in all the members of the truss  
(ii) the vertical deflection of the joint C.

[8M]

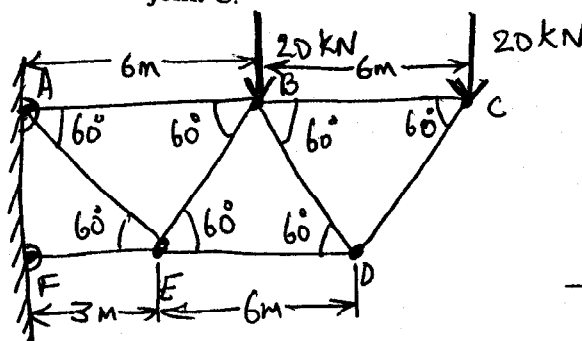


Fig. Q2

Q3. A 2m long cantilever column of square cross section  $100\text{mm} \times 100 \text{ mm}$  is to be made of steel ( $E=200 \text{ GN/m}^2$ ). Determine the critical load for buckling of the column.

[2M]

## PART B

Q4. For the given loading pattern (Fig. Q4), (i) find the reactions, (ii) expressions for the shear force and bending moment as a functions of distance along the beam, and (iii) sketch shear force and bending moment diagrams and label salient points. Indicate the sign convention employed.

[6M]

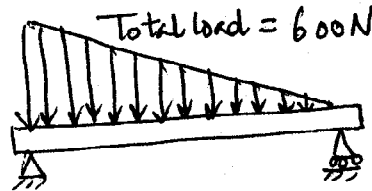


Fig. Q4

Q5. If the maximum principal stress is  $100 \text{ MN/m}^2$ , find (i)  $\sigma_y$ , (ii) and the angle which the principal stress axes makes with the  $xy$  axes for the case given below in Fig. Q5.

[5M]

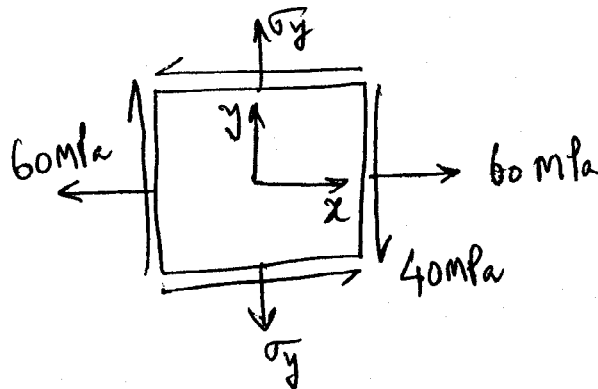


Fig Q5

Q6. Assume that a state of principal stresses developed at a point are shown in Fig. Q6. The stresses are directly proportional to a parameter " $\alpha$ ". What is " $\alpha$ " based on the Mises criterion if the yield stress is  $250 \text{ MPa}$ .

[2M]

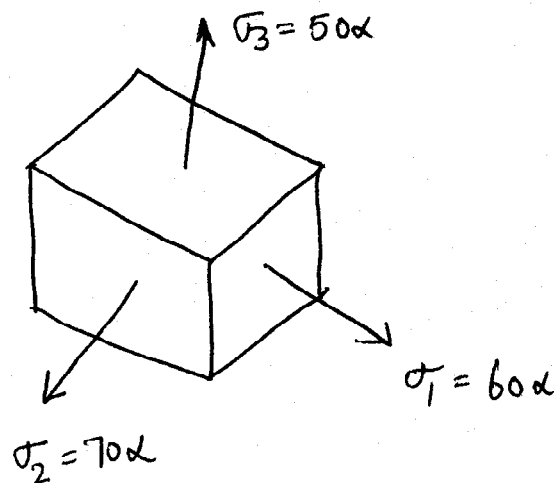
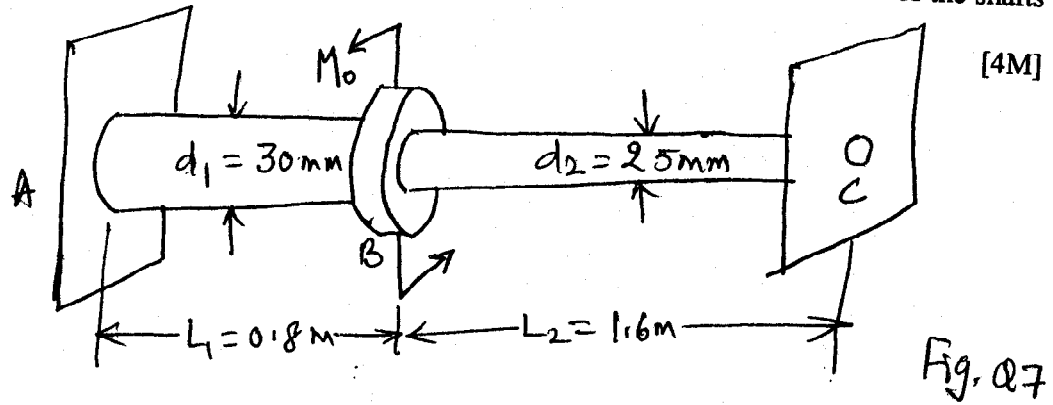


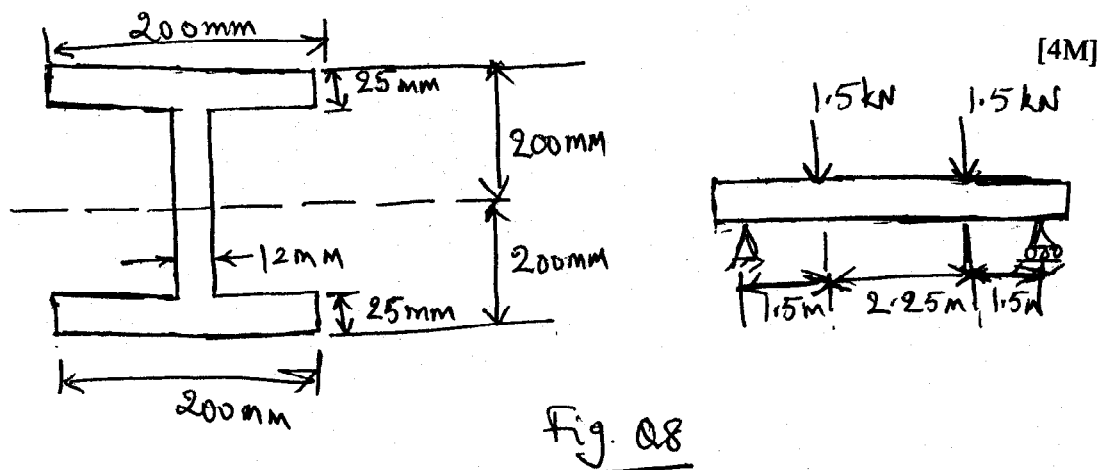
Fig. Q6

### PART C

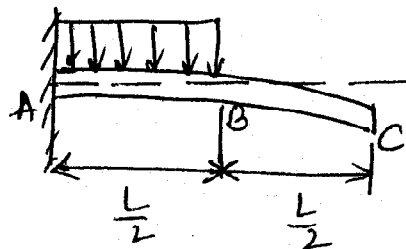
Q7. Two shafts AB and BC of the same material but different diameter are welded together at point B (Fig. Q7). Ends A and C are fastened securely so that the shafts cannot rotate at these points. An external twisting couple  $M_0 = 100 \text{ Nm}$  is applied to the shafts at point B. Assume the shear modulus  $G = 80 \text{ GN/m}^2$ . Find the twisting couples exerted on the ends of the shafts at A and C.



Q8. Consider the steel beam shown in Fig. Q8. Calculate the maximum bending stress in the beam.



Q9. Fig. Q9 shows a cantilever beam built-in at A and subjected to a uniformly distributed load of intensity  $w$  per unit length acting on the segment AB. Determine the deflection at C due to the distributed load in terms of the constant bending modulus  $EI$  and the dimensions shown.



ESUC221

Max Marks 20

Mechanics of Solids  
Test 2 - Make Makeup (Open Book)  
Weightage 2

Q1 An overhang beam is shown in Fig. 1.

i) Calculate the reactions

ii) Draw the Shear force diagram

iii) Determine the location and magnitude of maximum bending moment.

[8M]

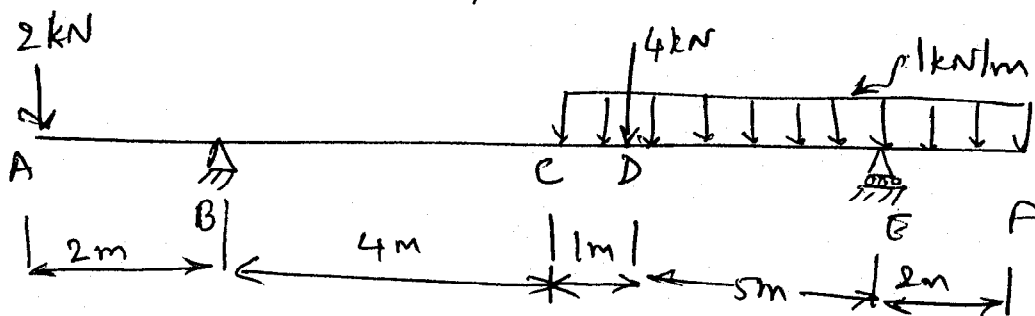
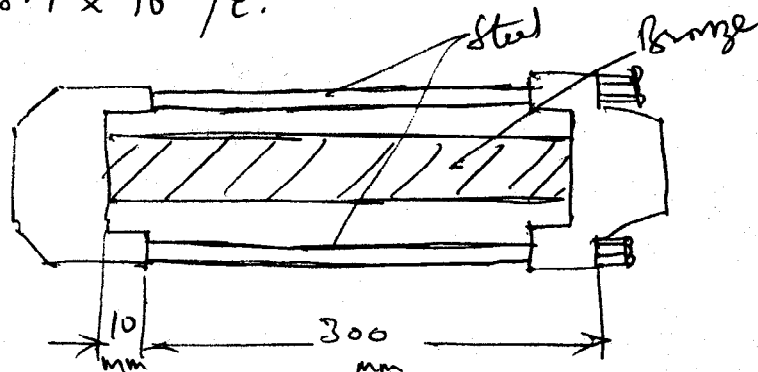


Fig. 1

Q2 A 30 mm diameter bronze cylinder is secured between a rigid cap and slab tightening two 20 mm diameter steel bolts. At 20°C, no deformation and stresses exist in the assembly. Determine the stresses in bronze and steel at 70°C. Use  $E_s = 200 \text{ GPa}$ ,  $E_b = 83 \text{ GPa}$ ,  $\alpha_s = 11.7 \times 10^{-6} / ^\circ\text{C}$ ,  $\alpha_b = 18.9 \times 10^{-6} / ^\circ\text{C}$ .

[6M]

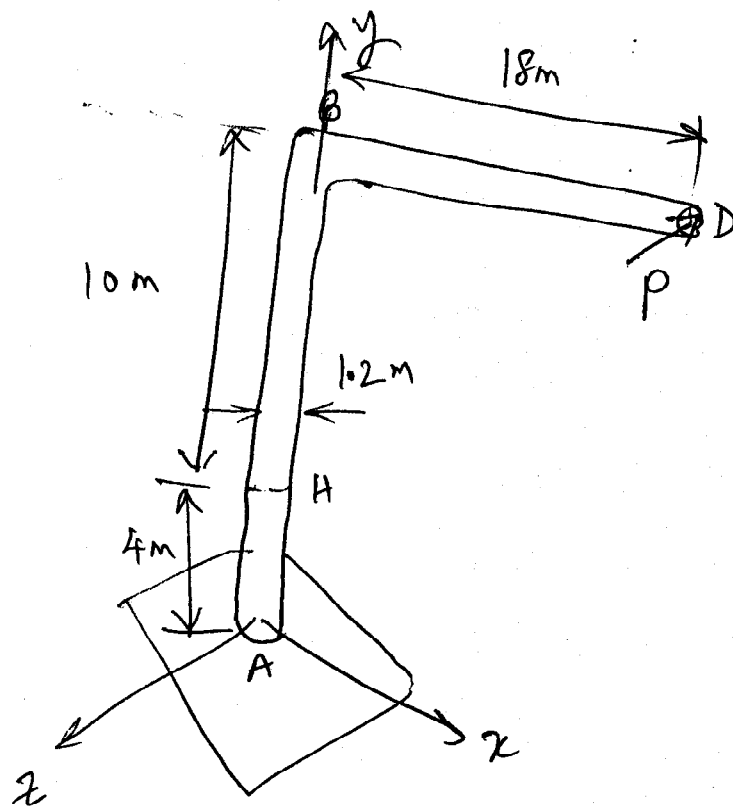


Q3

A single horizontal force  $P$  of magnitude  $150 \text{ kN}$  is applied at end  $D$  of lever  $ABD$ . Knowing that portion  $AB$  of the lever has a diameter of  $1.2 \text{ m}$ . Determine

(a) the normal and shearing stresses on an element located at point  $H$  and having sides parallel to  $x$  and  $y$  axes.

(b) the principal planes and principal stresses at point  $H$ .? [6m]





Q1. For the case shown in Fig. Q1, sketch the shear force and bending moment diagrams. Indicate sign convention employed and label important values. [8]

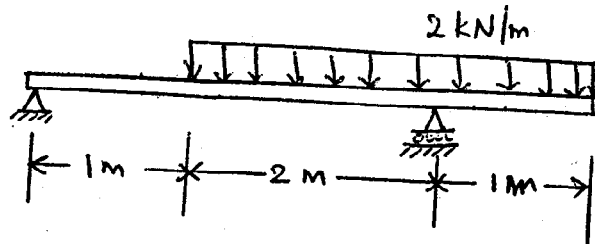


Fig. Q1

Q2. Consider a thin sheet pulled in its own plane so that the stress components with respect to the xy axes are as given in Fig. Q2. Construct the Mohr's circle and lay out the points x and y. Find the stress components with respect to ab axes which are inclined at  $60^\circ$  to the xy axes. Find the orientation of principal axes and axes of maximum shear. [6]

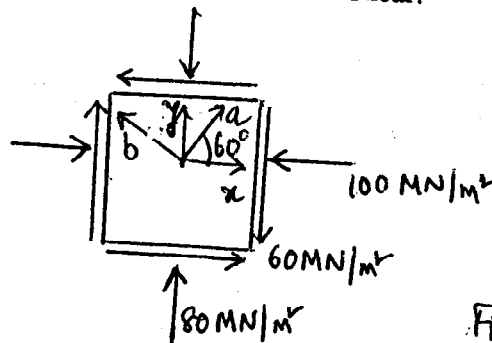


Fig Q2

Q3. A sheet of metal is deformed uniformly in its own plane so that the strain components related to set of xy axes are

$$\epsilon_x = 1000 \times 10^{-6}, \quad \epsilon_y = -600 \times 10^{-6}, \quad \gamma_{xy} = 800 \times 10^{-6}$$

Using Mohr's circle, find the magnitude of principal strains and orientation of principal strain directions. [4]

Q4. A 50 mm diameter steel rod has an initial length of 2 m. Determine the total strain along the axis of the rod after a tensile load of 25 kN is applied to the rod and the temperature of the rod increases by  $20^\circ\text{C}$ . For steel, Modulus of elasticity  $(E) = 200 \text{ GN/m}^2$ , and Coefficient of thermal expansion  $(\alpha) = 9 \times 10^{-6} / ^\circ\text{C}$ . [2]

**BITS, Pilani – Dubai Campus**  
**Knowledge Village, Dubai**  
**I Semester 2005 – 2006**

**TEST – I (Regular)**

Course No. : ES UC221.  
 Course Title : Mechanics of Solids.  
 Nature of Exam : Closed Book.  
 Weightage : 20 %  
 Duration : 50 minutes.  
 Date : 02.10.2005.

No. of Pages	= 2
No. of Questions	= 3

Note: Answer all questions.

- Q1. A cord connects two bodies A and B placed on an inclined plane as shown in fig.Q1. The coefficients of friction of body A is 0.15 and that of body B is 0.4. Determine
- the inclination of the plane to the horizontal
  - the tension in the cord when motion is about to take place down the inclined plane.

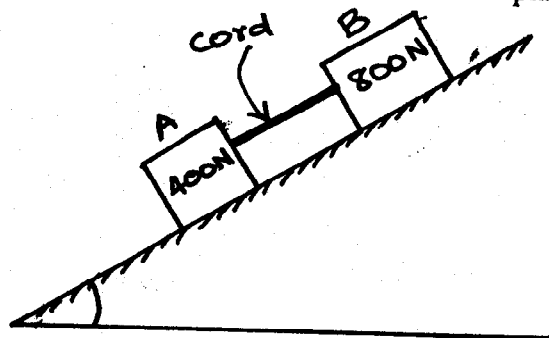


Fig. Q1.

(6 marks)

- Q2. In the pin-jointed cantilever truss shown in fig. Q2, all the members have a cross sectional area of  $350 \text{ mm}^2$  and elastic modulus  $205 \text{ G N/m}^2$ . Find:
- the forces in the rods due to the loads  $10 \text{ kN}$  &  $20 \text{ kN}$
  - the vertical deflection of the loaded joint A.

(8 marks)

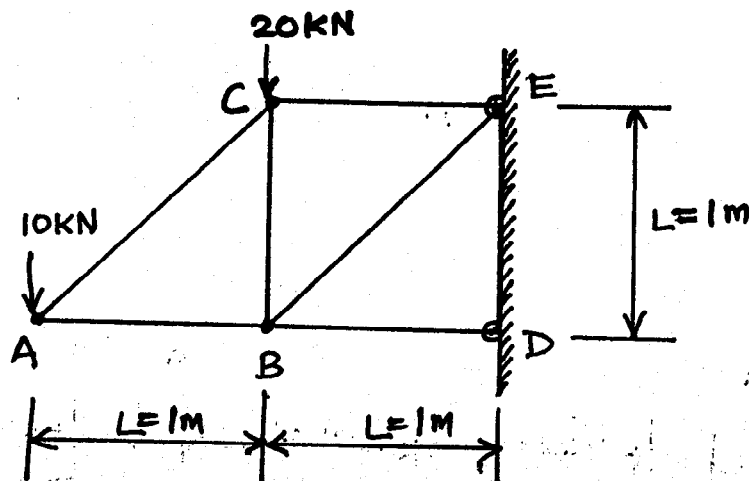


Fig. Q2.

P.T.O.

- Q3. A rigid beam AD is supported by a smooth pin at A and by horizontal bars (1) and (2) attached to the beam at points B and C respectively. Bar (1) is brass with cross sectional area of  $350 \text{ mm}^2$  and an elastic modulus of  $110 \text{ G N/m}^2$ . Bar (2) is steel with cross sectional area of  $175 \text{ mm}^2$  and an elastic modulus of  $190 \text{ G N/m}^2$ . A concentrated load of  $8 \text{ kN}$  is applied to the tip of the beam at D as shown in fig. Q3. Assume that the pin connections at B and C are ideal, meaning that there are no gaps. Compute the
- a. normal stresses in both the brass and steel bars.

(6 marks)

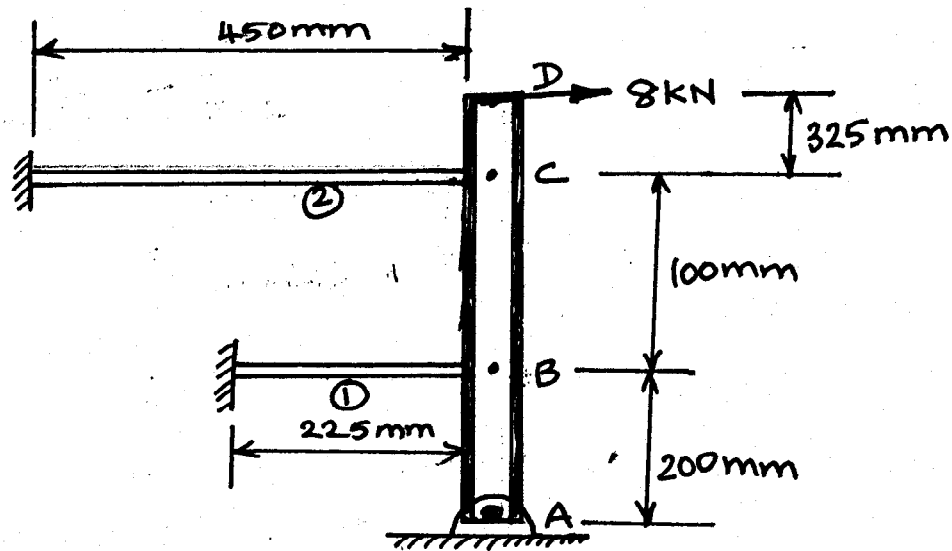


Fig. Q3.